

## AN APPROACH TO EVALUATING ALTERNATIVES FOR WIND POWER PLANT LOCATIONS

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### ABSTRACT

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Multi-criteria decision approaches are preferred for achieving multi-dimensional sustainable renewable energy goals. A more critical issue faced by the wind power industry is the selection of a location to tap prospective energy, which needs to be evaluated on multiple measures. In this paper, the aim is to assess and rank alternative wind power plant locations in Saudi Arabia. The approach presented here takes multiple criteria into consideration, such as wind speed, wind availability, site advantages, terrain details, risk and uncertainty, technology used, third party support, projected demand, types of customers, and government policies. A comparative analysis of feasible alternatives that satisfy all multi-criteria objectives is carried out. The results obtained are subjected to sensitivity analysis. Concepts such as 'threshold values' and 'attribute weights' make the approach more sensitive.

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### OPSOMMING

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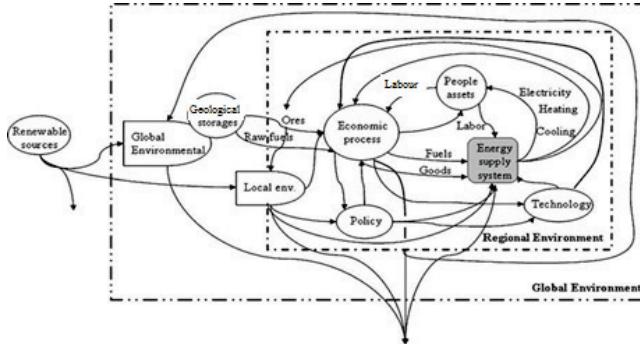
Multikriteria besluitnemingsbenaderings word verkies om multidimensionele, volhoubare en hernubare energie doelstellings te bereik. 'n Belangrike kwessie vir die windkragindustrie is die identifisering van 'n gesikte ligging wat onderhewig is aan verskeie kriteria. Hierdie artikel assesseer en rangskik verskeie potensiele windkragopwekking liggings in Saoedi-Arabië. Die voorgestelde benadering neem meervoudige kriteria, onder andere wind spoed en wind beskikbaarheid, ligging voordele, terrein detail, risiko en onsekerheid, die tegnologie wat gebruik word, derdeparty ondersteuning, geprojekteerde vraag, die tipe kliënte en regeringsbeleide, in ag. 'n Vergelykende analise van uitvoerbare alternatiewe wat aan al die kriteria doelstellings voldoen is uitgevoer. Die daaropvolgende resultate is dan aan 'n sensitiwiteitsanalise onderwerp. Konsepte soos drempelwaardes en eienskapgewigte maak die benadering meer sensitiief.

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## 1 INTRODUCTION

According to various published reports and expert opinions, it is evident that fossil fuels have an increasingly negative impact at a global level. Considering present global developments, sustainable renewable energy options play a vital role; and so choosing these options is being encouraged globally [1]. Common sources of renewable energy include solar energy, wind energy, and ocean energy. It is evident from the published literature that renewable energy is a focus of planning, implementation, and development activities in local and global energy programmes [2, 3]. Decision-making in the renewable energy sector is very complex and difficult (see Figure 1), where multiple criteria and their respective objectives have to be considered in the decision analysis [4].

Researchers and practitioners have adopted multi-criteria decision analysis in a number of industrial applications – for example the fuzzy approach in manufacturing technology investment decisions [5]; the fuzzy analytical hierarchy approach [6] for evaluating energy plans; and the analytical hierarchy approach [7] to justify non-financial decisions about manufacturing. Similarly, researchers



**Figure 1: Sustainable renewable energy sector control factors [1]**

have adopted multi-criteria decision approaches [8] in the evaluation of water resource alternatives in addition to energy systems.

A more critical issue faced by the top management is the selection of a location to tap prospective wind energy that needs to be evaluated on multiple measures. Decision-makers may have to say 'yes' or 'no' to a particular option, and justify their decision. To do this, they have to conduct a comparative analysis of the alternatives. The purpose of the current study is to make decisions about the location of future wind energy generation facilities using a multi-criteria decision-making model. Hence, in this paper, an attempt is made to present an approach to assessing and ranking alternative wind power plant locations for a Saudi Arabian power generation company. A decision tree is developed for strategic selection of a wind power plant location. In order to overcome the challenge of ranking alternative locations, the 'elimination and choice translating' approach, based on concord and disconcord indices, is proposed. The adopted approach uses indifference preference analysis, which is based on the concordance index and on threshold values.

## 2 LITERATURE REVIEW

Multi-criteria decision-making (MCDM) approaches are currently gaining popularity in energy demand management. These approaches can handle both qualitative and quantitative criteria. It is evident that one has to evaluate the problems raised by conflicting and multiple objectives. It is also evident that experts have great difficulty in intuitively combining information in appropriate ways. Because of the limitations of such an intuitive decision-making process, discrete multi-criteria approaches are needed to help determine the worth of multi-attribute alternatives [6]. The first step in the application of any multi-criteria decision-making approach is the elimination of all dominant alternatives; and the final step is to select only one non-dominant alternative. A concise review of the most favoured multi-criteria decision-making approaches is presented below.

**Analytic hierarchy process (AHP):** A multi-criteria decision-making approach introduced by Saaty [9]. The approach needs a decision tree with the goal at the top level, criteria and sub-criteria on the middle levels, and the alternatives at the bottom. In AHP, the experts and decision-makers do pairwise comparisons and select the best alternative according to the highest rank between alternatives. The drawback of the approach is its unidirectional relationship characteristic that cannot handle the complexity of many problems.

**Analytic network process (ANP):** The ANP methodology is a general form of the AHP, and was also introduced by Saaty [10]. ANP partly overcomes the drawback of AHP, and deals with the problem as a network of complex relationships between alternatives and criteria where all the elements are connected. To understand uses of ANP, refer to Pablo *et al.* [11].

**The preference ranking organisation method for enrichment evaluation (PROMETHEE):** This method uses positive and negative outranking flows to rank the alternatives. Both flows do not usually produce the same rankings. Subsequently, the approach considers the net outranking flow to perform a pair-wise comparison of alternatives in order to rank them against a number of criteria [12].

The elimination and choice translating reality (ELECTRE): The ELECTRE approach is focused on the dominance relationships between alternatives. It is based on the outranking relationships, and uses thresholds of indifference and preference to do pair-wise comparisons between alternatives [13]. Decision-makers prefer the ELECTRE approach over the other approaches due to its ability to incorporate the fuzzy nature of decision-making.

The technique for order preference by similarity to ideal solutions (TOPSIS): The basic concept of the TOPSIS approach is to select an alternative that is the shortest distance from the negative ideal solution [14]. The approach demarcates the positive ideal and negative ideal solutions. The Euclidean distance approach is used to evaluate the relative closeness of the alternatives to the ideal solution.

In general, multi-criteria decision-making approaches have the following basic steps [15]: (a) formulate the decision tree using alternatives, criteria, and sub-criteria; (b) determine the relative importance of the criteria and the impacts of the alternatives on these criteria; (c) process the numerical values to determine a ranking of each alternative, then apply value judgment about acceptable tradeoffs and evaluation; and (d) calculate the final ranking and make a decision.

Researchers in the area of energy planning have discussed and compared multi-criteria decision-making methods, and presented their applications and expected outcomes [16]. It is evident that multi-criteria decision-making applications are preferred in the selection of power plant locations [17] and renewable energy [18], and in energy transportation planning [19-20]. Özkan *et al.* [21] make use of a hybrid multi-criteria approach for selection among energy storage alternatives. Arce *et al.* [22] published a review on the use of multi-criteria analysis in the evaluation of sustainable energy options. Wanderer and Herle [23] used a web-based multi-criteria approach for solar plant location preferences. Similarly, a gray grade approach [22], an analytical hierarchy approach [24], and a fuzzy approach [25] are used in rural area energy planning. Sola and de Miranda Mota [26] presented the multi-criteria PROMETHEE and Geometrical Analysis for Interactive decision Aid (GAIA) approaches particularly for industrial energy management. The graph theory approach is used to evaluate and select energy technologies [27]. Researchers have presented various applications of multi-criteria approaches as case studies. For example, Zhang *et al.* [28] evaluated clean energy alternatives in China; Ümran Şengül *et al.* [29] used an approach based on the similarity index to rank energy supply alternatives in Turkey; Tahri *et al.* [30] evaluated solar farm locations in Morocco; and Sharma *et al.* [31] made use of the fuzzy decision approach to select energy resources in India.

From the literature it is evident that most approaches with multi-objective performance criteria need a systematic analysis at multiple decision levels, from tactical to operational. In order to overcome this challenge, the elimination and choice translating approach based on concord and disconcord indices is proposed. Details of the case in point, and the steps of the approach, are presented in the next section.

### 3 PROBLEM DEFINITION

In the light of global environmental requirements, a power industry in Saudi Arabia is interested in making use of a sustainable renewable wind energy option for power generation. The company generates and transmits power to major customers in Saudi Arabia and other Gulf countries. A critical issue that has been flagged is the selection of a location to tap prospective wind energy that needs to be evaluated on multiple measures. Five alternative locations were identified by the top management. It was evident that multiple criteria needed to be considered in selecting the best location. There might be multiple alternative solutions, resulting in exactly the same state of affairs. A decision tree that has multiple criteria is proposed to resolve this (see Figure 2).

In the decision tree, the first level has a statement of the objective. The subsequent levels have criteria, and the last level represents the alternative options. The criteria that are eventually suggested to evaluate the power station are grouped into wind availability, site advantages, topography details, technology used, risk and uncertainty, third party support, and government policies. Seventeen criteria in all are suggested to evaluate wind-energy power plant locations (see Figure 2).

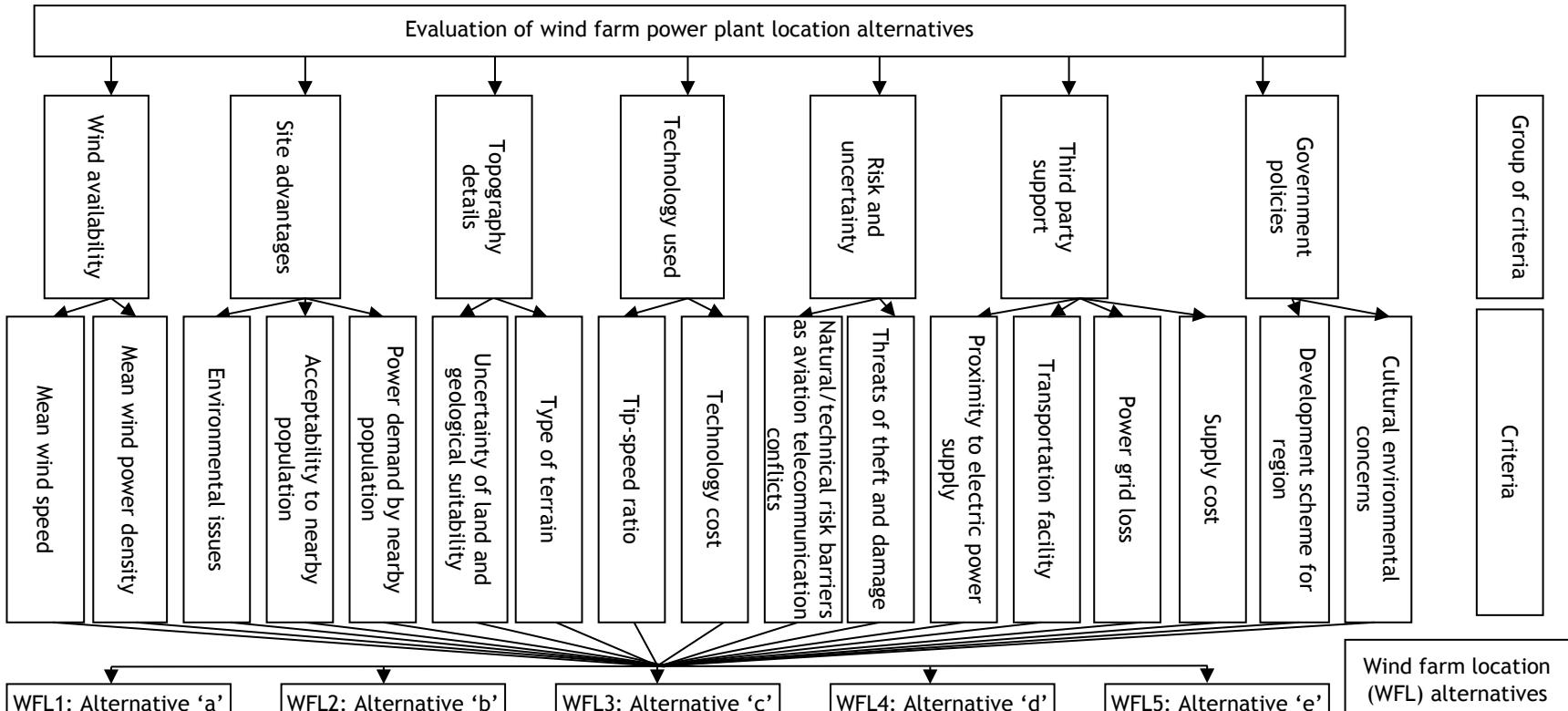


Figure 2: The proposed hierarchical decision model for evaluation of wind farm plant locations

#### 4 MULTI-CRITERIA DECISION-MAKING (MCDM) APPROACH

The procedural steps followed in the approach are presented below.

**Step 1:** Collect relevant data for each alternative: The presented approach uses an evaluation scoring scale of 1 to 5 (see Table 1). A menu-driven online resource is used to obtain expert opinion. For example, an expert's scores for alternative 'a' (WFL1) correspond with 'k' criteria ( $k \in 1$  to 17; see Table 1). This is presented in matrix form in Equation 1:

$$S_a^k = \begin{bmatrix} k \rightarrow & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 & 15 & 16 & 17 \\ a:WFL1 & 2 & 3 & 2 & 5 & 5 & 5 & 4 & 3 & 3 & 4 & 5 & 4 & 3 & 3 & 3 & 5 & 3 \end{bmatrix} \quad (1)$$

Using the criteria set out in Table 1 below, the matrix in Eq 1 yields this information for wind farm location alternative WFL1: average wind speed is in the range of 4 m/sec to 5 m/sec; average wind power density is in the range of 400 to 500 W/sq.meter; the location has moderate environmental issues; acceptability to the local community is excellent; community power demand is high; the terrain is found to be flat; the location has good geological suitability; there is a decision to invest in moderate technology cost and tip-speed ratio; there are minor risk barriers and no threat of thefts; proximity to an alternative power supply is in the range of two to 10 kms; there are moderate transportation and supply costs; government has announced a development scheme for the region; and the site has average environmental concerns.

The expert scores considered when evaluating five wind farm location alternatives ( $j: a$  to  $e$ ) are presented in matrix form in Equation 2:

$$S_j^k = \begin{bmatrix} \downarrow j/k \rightarrow & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 & 15 & 16 & 17 \\ a:WFL1 & 2 & 3 & 2 & 5 & 5 & 5 & 4 & 3 & 3 & 4 & 5 & 4 & 3 & 3 & 3 & 5 & 3 \\ b:WFL2 & 4 & 5 & 3 & 2 & 3 & 3 & 2 & 3 & 3 & 2 & 1 & 1 & 4 & 3 & 5 & 3 & 2 \\ c:WFL3 & 3 & 4 & 3 & 2 & 5 & 3 & 5 & 3 & 3 & 2 & 3 & 2 & 3 & 4 & 4 & 4 & 3 \\ d:WFL4 & 3 & 3 & 5 & 5 & 5 & 5 & 4 & 3 & 3 & 5 & 3 & 3 & 5 & 5 & 3 & 5 & 4 \\ e:WFL5 & 2 & 3 & 4 & 3 & 3 & 2 & 3 & 3 & 3 & 2 & 3 & 2 & 3 & 2 & 3 & 3 & 4 \end{bmatrix} \quad (2)$$

**Step 2:** Define weightings against criteria.

This approach requires criteria weightings, and thus the weighting for each criterion (see Figure 2) is chosen based on the opinions of experts. One group of experts was of the opinion that equal weighting should be assigned to all criteria. A second group of experts stressed that a greater weighting should be assigned to the availability of wind speed and density. Another group of experts stated that a high weighting should be given to demand for power, power supply cost, wind speed, and wind density. Some experts chose to give a higher weighting to the environment and technology, and a low weighting to cost and risk.

A number of experts were asked to assign a weighting to each criterion out of 100. Using their weightings, three sets of weightings were selected (see Table 2) and used in the sensitivity analysis.

**Step 3:** Determine concord and discord indices

As presented in steps 1 and 2 above, the experts' scores for each alternative and set of criteria weightings are used to calculate the concord and discord indices. The concord index 'CI' is defined for each pair of alternatives, and is presented in Equation 3.

**Table 1: Criteria evaluation scale**

		1 to 5 scale to evaluate each criterion				
Grouping of criteria	Criteria ( $k \in 1 \text{ to } 17$ )	1	2	3	4	5
Wind availability	1. Average wind speed	< 4 m/s	4 - 5 m/s	5 - 6 m/s	6 - 7 m/s	> 7 m/s
	2. Average wind power density	< 300 W/m <sup>2</sup>	300-400 W/m <sup>2</sup>	400 - 500 W/m <sup>2</sup>	500 - 600 W/m <sup>2</sup>	> 600 W/m <sup>2</sup>
Site advantages	3. Environmental issues	Extensive	Moderate	Average	Minor	None
	4. Acceptability	Poor	Marginal	Satisfactory	Good	Excellent
	5. Power demand	Low		Moderate		High
Topography details	6. Type of terrain	Rugged	Complex	Moderate	Rolling	Flat
	7. Geological suitability	Poor	Marginal	Satisfactory	Good	Excellent
Technology used	8. Technology cost	High		Moderate		Low
	9. Tip-speed ratio	High		Moderate		Low
Risk and uncertainty	10. Threats of theft and damage	Extensive	Moderate	Average	Minor	None
	11. Natural/technical risk barriers	Extensive		Moderate		None
Third party support	12. Proximity to electric power supply	> 40 Km	20 - 40 Km	10 - 20 Km	2 - 10 Km	< 2 Km
	13. Transportation facility	Poor	Marginal	Upgradable	Good	Excellent
	14. Power grid loss	Poor	Marginal	Satisfactory	Good	Excellent
	15. Supply cost	High		Moderate		Low
Government policies	16. Development scheme for region	None		Moderate		High
	17. Cultural environmental concerns	Extensive	Moderate	Average	Minor	None

Note: For example, at a given wind farm location, if the average wind speed is found to be less than 4 m/s, then the location is assigned a minimum score of 1. Similarly, if the average wind speed is found to be more than 7 m/s, then that location is assigned a maximum score of 5.

**Table 2: Criteria weightings**

Criteria ( $k \in 1$ to 17)	Criteria weighting ( $W_k$ ) out of 100		
	Set 1	Set 2	Set 3
1. Average wind speed m/s	60	90	90
2. Average wind power density W/m <sup>2</sup>	60	90	90
3. Environmental issues	60	90	60
4. Acceptability	60	50	60
5. Power demand	60	60	90
6. Type of terrain	60	60	60
7. Geological suitability	60	50	60
8. Technology cost	60	30	90
9. Tip-speed ratio	60	60	60
10. Threats of theft and damage	60	60	25
11. Natural/technical risk barriers	60	60	30
12. Proximity to electric power supply	60	60	25
13. Transportation facility	60	60	25
14. Power grid loss	60	90	25
15. Supply cost	60	60	90
16. Development scheme for region	60	25	70
17. Cultural environmental concerns	60	25	70
Total weighting (W)	1020	1020	1020

$$CI = \begin{bmatrix} \downarrow j \rightarrow & a:WFL1 & b:WFL2 & c:WFL3 & d:WFL4 & e:WFL5 \\ a:WFL1 & * & CI_{ab} & CI_{ac} & CI_{ad} & CI_{ae} \\ b:WFL2 & CI_{ba} & * & CI_{bc} & CI_{bd} & CI_{be} \\ c:WFL3 & CI_{ca} & CI_{cb} & * & CI_{cd} & CI_{ce} \\ d:WFL4 & CI_{da} & CI_{db} & CI_{dc} & * & CI_{de} \\ e:WFL5 & CI_{ea} & CI_{eb} & CI_{ec} & CI_{ed} & * \end{bmatrix} \quad (3)$$

The value of each CI element in Equation 3 above is obtained using equations (4) to (6) below:

$$W = \sum_{k=1}^{17} W_k \quad (4)$$

$$\left[ \begin{array}{l} \{CI_{ab}^k = 1 \text{ if } S_a^k \geq S_b^k\} \{CI_{ab}^k = 0 \text{ if } S_a^k < S_b^k\} \{CI_{ba}^k = 1 \text{ if } S_b^k \geq S_a^k\} \{CI_{ba}^k = 0 \text{ if } S_b^k < S_a^k\} \\ \{CI_{ac}^k = 1 \text{ if } S_a^k \geq S_c^k\} \{CI_{ac}^k = 0 \text{ if } S_a^k < S_c^k\} \{CI_{ca}^k = 1 \text{ if } S_c^k \geq S_a^k\} \{CI_{ca}^k = 0 \text{ if } S_c^k < S_a^k\} \\ \{CI_{ad}^k = 1 \text{ if } S_a^k \geq S_d^k\} \{CI_{ad}^k = 0 \text{ if } S_a^k < S_d^k\} \{CI_{da}^k = 1 \text{ if } S_d^k \geq S_a^k\} \{CI_{da}^k = 0 \text{ if } S_d^k < S_a^k\} \\ \{CI_{ae}^k = 1 \text{ if } S_a^k \geq S_e^k\} \{CI_{ae}^k = 0 \text{ if } S_a^k < S_e^k\} \{CI_{ea}^k = 1 \text{ if } S_e^k \geq S_a^k\} \{CI_{ea}^k = 0 \text{ if } S_e^k < S_a^k\} \\ \{CI_{bc}^k = 1 \text{ if } S_b^k \geq S_c^k\} \{CI_{bc}^k = 0 \text{ if } S_b^k < S_c^k\} \{CI_{cb}^k = 1 \text{ if } S_c^k \geq S_b^k\} \{CI_{cb}^k = 0 \text{ if } S_c^k < S_b^k\} \\ \{CI_{bd}^k = 1 \text{ if } S_b^k \geq S_d^k\} \{CI_{bd}^k = 0 \text{ if } S_b^k < S_d^k\} \{CI_{db}^k = 1 \text{ if } S_d^k \geq S_b^k\} \{CI_{db}^k = 0 \text{ if } S_d^k < S_b^k\} \\ \{CI_{be}^k = 1 \text{ if } S_b^k \geq S_e^k\} \{CI_{be}^k = 0 \text{ if } S_b^k < S_e^k\} \{CI_{eb}^k = 1 \text{ if } S_e^k \geq S_b^k\} \{CI_{eb}^k = 0 \text{ if } S_e^k < S_b^k\} \\ \{CI_{cd}^k = 1 \text{ if } S_c^k \geq S_d^k\} \{CI_{cd}^k = 0 \text{ if } S_c^k < S_d^k\} \{CI_{dc}^k = 1 \text{ if } S_d^k \geq S_c^k\} \{CI_{dc}^k = 0 \text{ if } S_d^k < S_c^k\} \\ \{CI_{ce}^k = 1 \text{ if } S_c^k \geq S_e^k\} \{CI_{ce}^k = 0 \text{ if } S_c^k < S_e^k\} \{CI_{ec}^k = 1 \text{ if } S_e^k \geq S_c^k\} \{CI_{ec}^k = 0 \text{ if } S_e^k < S_c^k\} \\ \{CI_{de}^k = 1 \text{ if } S_d^k \geq S_e^k\} \{CI_{de}^k = 0 \text{ if } S_d^k < S_e^k\} \{CI_{ed}^k = 1 \text{ if } S_e^k \geq S_d^k\} \{CI_{ed}^k = 0 \text{ if } S_e^k < S_d^k\} \end{array} \right] \quad (5)$$

$$\left[ \begin{array}{l} \{CI_{ab} = \frac{1}{W} \sum_{k=1}^m W_k CI_{ab}^k\} \{CI_{ba} = 1 - CI_{ab}\} \{CI_{ac} = \frac{1}{W} \sum_{k=1}^m W_k CI_{ac}^k\} \{CI_{ca} = 1 - CI_{ac}\} \\ \{CI_{ad} = \frac{1}{W} \sum_{k=1}^m W_k CI_{ad}^k\} \{CI_{da} = 1 - CI_{ad}\} \{CI_{ae} = \frac{1}{W} \sum_{k=1}^m W_k CI_{ae}^k\} \{CI_{ea} = 1 - CI_{ae}\} \\ \{CI_{bc} = \frac{1}{W} \sum_{k=1}^m W_k CI_{bc}^k\} \{CI_{cb} = 1 - CI_{bc}\} \{CI_{bd} = \frac{1}{W} \sum_{k=1}^m W_k CI_{bd}^k\} \{CI_{db} = 1 - CI_{bd}\} \\ \{CI_{be} = \frac{1}{W} \sum_{k=1}^m W_k CI_{be}^k\} \{CI_{eb} = 1 - CI_{be}\} \{CI_{cd} = \frac{1}{W} \sum_{k=1}^m W_k CI_{cd}^k\} \{CI_{dc} = 1 - CI_{cd}\} \\ \{CI_{ce} = \frac{1}{W} \sum_{k=1}^m W_k CI_{ce}^k\} \{CI_{ec} = 1 - CI_{ce}\} \{CI_{de} = \frac{1}{W} \sum_{k=1}^m W_k CI_{de}^k\} \{CI_{ed} = 1 - CI_{de}\} \end{array} \right] \quad (6)$$

In Equations (3) to (6) above,  $S_a^k$  implies alternative 'a' scores for each criterion k;  $CI_{ab}^k$  is the concord index after comparing alternative 'a' with 'b' for a criterion 'k';  $CI_{ab}$  implies an aggregate concord index after comparing alternative 'a' with 'b' for all criteria ( $k \in 1$  to 17); and  $W_k$  represents the set of criteria weightings defined by the decision-maker (see Table 2). Thus concord indices are obtained

(using Equations 3 to 6) for each pair of alternative wind-energy farm locations. An example of how these indices are obtained for a pair is presented below.

And

$$CI_{ba} = 1 - CI_{ab} = 1 - 0.706 = 0.294$$

Thus each set of criteria weightings (see Table 2) with concord indices for each possible twenty pairs of alternatives was obtained. They are presented below.

$$CI_{\text{for weight Set1}} = \left[ \begin{array}{cccccc} \downarrow j \rightarrow & a: \text{WFL1} & b: \text{WFL2} & c: \text{WFL3} & d: \text{WFL4} & e: \text{WFL5} \\ a: \text{WFL1} & * & CI_{ab} = 0.706 & CI_{ac} = 0.647 & CI_{ad} = 0.647 & CI_{ae} = 0.882 \\ b: \text{WFL2} & CI_{ba} = 0.294 & * & CI_{bc} = 0.588 & CI_{bd} = 0.294 & CI_{be} = 0.647 \\ c: \text{WFL3} & CI_{ca} = 0.353 & CI_{cb} = 0.412 & * & CI_{cd} = 0.471 & CI_{ce} = 0.824 \\ d: \text{WFL4} & CI_{da} = 0.353 & CI_{db} = 0.706 & CI_{dc} = 0.529 & * & CI_{de} = 1.000 \\ e: \text{WFL5} & CI_{ea} = 0.118 & CI_{eb} = 0.353 & CI_{ec} = 0.176 & CI_{ed} = 0.000 & * \end{array} \right] \quad (7)$$

$$CI_{\text{for weight Set2}} = \begin{bmatrix} \downarrow j \rightarrow & a: WFL1 & b: WFL2 & c: WFL3 & d: WFL4 & e: WFL5 \\ a: WFL1 & * & CI_{ab} = 0.618 & CI_{ac} = 0.539 & CI_{ad} = 0.593 & CI_{ae} = 0.887 \\ b: WFL2 & CI_{ba} = 0.382 & * & CI_{bc} = 0.637 & CI_{bd} = 0.324 & CI_{be} = 0.672 \\ c: WFL3 & CI_{ca} = 0.461 & CI_{cb} = 0.363 & * & CI_{cd} = 0.490 & CI_{ce} = 0.838 \\ d: WFL4 & CI_{da} = 0.407 & CI_{db} = 0.676 & CI_{dc} = 0.510 & * & CI_{de} = 1.000 \\ e: WFL5 & CI_{ea} = 0.113 & CI_{eb} = 0.328 & CI_{ec} = 0.162 & CI_{ed} = 0.000 & * \end{bmatrix} \quad (8)$$

$\text{Cl}_{\text{for weight Set3}}$	$j \rightarrow$	1: WFL1	2: WFL2	3: WFL3	4: WFL4	5: WFL5
1: WFL1	*	$\text{Cl}_{ab} = 0.652$	$\text{Cl}_{ac} = 0.593$	$\text{Cl}_{ad} = 0.711$	$\text{Cl}_{ae} = 0.873$	
2: WFL2	$\text{Cl}_{ba} = 0.348$	*	$\text{Cl}_{bc} = 0.637$	$\text{Cl}_{bd} = 0.412$	$\text{Cl}_{be} = 0.701$	
3: WFL3	$\text{Cl}_{ca} = 0.407$	$\text{Cl}_{cb} = 0.363$	*	$\text{Cl}_{cd} = 0.588$	$\text{Cl}_{ce} = 0.814$	
4: WFL4	$\text{Cl}_{da} = 0.289$	$\text{Cl}_{db} = 0.588$	$\text{Cl}_{dc} = 0.412$	*	$\text{Cl}_{de} = 1.000$	
5: WFL5	$\text{Cl}_{ea} = 0.127$	$\text{Cl}_{eb} = 0.299$	$\text{Cl}_{ec} = 0.186$	$\text{Cl}_{ed} = 0.000$	*	

The approach does not rely only on concord index CI: the discord index is preferred. The discord index 'DI' is calculated for each pair of alternatives, and presented in Equation 10.

$$DI = \begin{bmatrix} \downarrow j \rightarrow & a & b & c & d & e \\ a & * & DI_{ab} & DI_{ac} & DI_{ad} & DI_{ae} \\ b & DI_{ba} & * & DI_{bc} & DI_{bd} & DI_{be} \\ c & DI_{ca} & DI_{cb} & * & DI_{cd} & DI_{ce} \\ d & DI_{da} & DI_{db} & DI_{dc} & * & DI_{de} \\ e & DI_{ea} & DI_{eb} & DI_{ec} & DI_{ed} & * \end{bmatrix}, \quad (10)$$

where 'j' represents alternatives from 'a' to 'e', and 'k' represents the set of evaluation criteria.  $Dl_{ab}$  is the discord index value when alternative 'a' is compared with alternative 'b' across all criteria 'k';  $Dl_{ba}$  is the discord index value when alternative 'b' is compared with alternative 'a' across all criteria 'k'. The value of each element in the DI matrix above is obtained using Equation 11.

$$\left[ \begin{array}{l} DI_{ab} = \max \left\{ \frac{S_a^k - S_b^k}{\max S^k} \right\} \text{ for } k \in 1 \text{ to } m \text{ and } DI_{ba} = 1 - DI_{ab} \\ \vdots \\ DI_{ae} = \max \left\{ \frac{S_a^k - S_e^k}{\max S^k} \right\} \text{ for } k \in 1 \text{ to } m \text{ and } DI_{ea} = 1 - DI_{ae} \end{array} \right] \quad (11)$$

In the equation above, for a given performance criterion ‘k’,  $\max S^k$  represents the maximum criterion score among all the alternatives. Thus, for each pair of alternatives, the discord index DI is calculated and the maximum value is assigned to that pair of alternatives.

For example,

$S_j^k \downarrow j/k \rightarrow$	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
a:WFL1	2	3	2	5	5	5	4	3	3	4	5	4	3	3	3	5	3
b:WFL2	4	5	3	2	3	3	2	3	3	2	1	1	4	3	5	3	2
c:WFL3	3	4	3	2	5	3	5	3	3	2	3	2	3	4	4	4	3
d:WFL4	3	3	5	5	5	5	4	3	3	5	3	3	5	5	3	5	4
e:WFL5	2	3	4	3	3	2	3	3	3	2	3	2	3	2	3	3	4
$S^k = \max(S_j^k)$	4	5	5	5	5	5	5	3	3	5	5	4	5	5	5	5	4
$\frac{S_a^k - S_b^k}{\max S^k}$	-0.5	-0.4	-0.2	0.6	0.4	0.4	0.4	0	0	0.4	0.8	0.75	-0.2	0	-0.4	0.4	0.25

$DI_{ab} = \max \left\{ \frac{S_a^k - S_b^k}{\max S^k} \right\} = 0.8$  and  $DI_{ba} = 1 - 0.8 = 0.2$ , thus DIs are obtained for each pair. The obtained values of DI are presented in Equation 12 below:

$\downarrow j \rightarrow$	a	b	c	d	e
a	*	0.8	0.6	0.4	0.6
b	0.2	*	0.25	0.4	0.5
c	0.4	0.75	*	0.2	0.4
d	0.6	0.6	0.8	*	0.6
e	0.4	0.5	0.6	0.4	*

(12)

#### Step 4: Set threshold value

Next, the decision-maker has to set the threshold values ( $\Theta$  and  $\emptyset$ ). They are used to draw the outranking relationship graph. These values are used to decide the preference relationship for a given pair of alternatives. These pairs of alternatives exhibit performance scores  $S_a^k$  and  $S_b^k$  for a given criterion ‘k’. The three preference relationships are drawn using threshold values ( $\Theta$  and  $\emptyset$ ) as follows:

- If  $S_a^k - S_b^k > \Theta$ , then alternative ‘a’ is strongly preferred over alternative ‘b’. In other words ‘a is better than b’.
- If  $\Theta < S_a^k - S_b^k \leq \emptyset$ , then alternative ‘a’ is not preferred over alternative ‘b’; that is, ‘b is better than a’.
- If  $|S_a^k - S_b^k| \leq \emptyset$ , then alternatives ‘a’ and ‘b’ are ‘equally preferred’. In other words, ‘a is at least as good as b’ or ‘a is not worse than b’.

These relationships were drawn for all criteria and then synthesised to obtain the outranking relationship. For threshold coefficient values, see Table 3. These multiple values are used further for the sensitivity analysis.

Table 3: Threshold coefficient values adopted in the study

Parameters	Levels	Values
Threshold value $\Theta$	4	0.8, 0.7, 0.6 & 0.5
Threshold value $\emptyset$	4	0.2, 0.3, 0.4 & 0.5

### Step 5: Set outranking relationship and draw kernel graph

Given two alternatives, ‘a’ and ‘b’, the outranking relationship between them is drawn using the concord index  $CI_{ab}$ , the discord index  $DI_{ab}$ , and the threshold values ( $\Theta$  and  $\emptyset$ ), because if  $CI_{ab} \geq \Theta$  and  $DI_{ab} \leq \emptyset$ , then alternative ‘a’ is preferred over alternative ‘b’; that is, ‘a’ outranks ‘b’. This preference is highlighted graphically in a kernel graph, in which the choice of alternative ‘a’ over alternative ‘b’ is represented by an arrow ‘ $\rightarrow$ ’ from ‘a’ to ‘b’. Such outranking relationships are drawn for all pairs of alternatives for preset threshold values.

For example, for a selected set of threshold values ( $\Theta = 0.6$  and  $\emptyset = 0.4$ ), using matrix of CI (see Equation 7) and DI matrix (see Equation 10), the outranking relationship graph kernel is drawn. It can be concluded that the pairs that satisfy the condition  $CI \geq 0.6$  are (WFL1, WFL2), (WFL1, WFL3), (WFL1, WFL4), (WFL1, WFL5), (WFL2, WFL5), (WFL3, WFL5), (WFL4, WFL2), and (WFL4, WFL5); and the pairs that satisfy the condition  $DI \leq 0.4$  are (WFL1, WFL4), (WFL2, WFL1), (WFL2, WFL3), (WFL2, WFL4), (WFL3, WFL1), (WFL3, WFL4), (WFL3, WFL5), (WFL5, WFL1), and (WFL5, WFL4).

Now, to draw the outranking relationship kernel graph, pairs of alternatives that satisfy both  $CI \geq 0.60$  and  $DI \leq 0.40$  are selected. In the above case, for the pairs (WFL1, WFL4) and (WFL3, WFL5), the concord index is more than 0.8 and the discord index is less than 0.40; so only two pairs satisfy. The outranking relationship kernel graph is drawn between these alternatives, as shown in Figure 3. The preference of alternative WFL3 over alternative WFL5 is represented by an arrow  $\rightarrow$  from WFL3 to WFL5. And the preference of alternative WFL1 over alternative WFL4 is also represented by an arrow  $\rightarrow$  from WFL1 to WFL4. From this graph, it is said that the alternatives WFL4 and WFL5 are the least preferred among the alternatives. In the same way, if decision-makers change the preference threshold values  $\Theta$  to 0.5 and  $\emptyset$  to 0.5, the outranking relationship kernel graph is drawn between these alternatives (see Figure 4). From this graph, it is said that WFL2 is preferred over WFL3 and WFL5, while WFL1 is preferred over WFL4. WFL4 and WFL5 thus seem to be the worst choices.

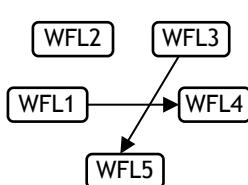


Figure 3: Outranking relationship kernel graph for threshold values

$$\Theta = 0.60 \text{ and } \emptyset = 0.40$$

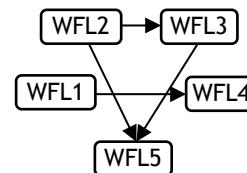


Figure 4: Outranking relationship kernel graph for threshold values

$$\Theta = 0.5 \text{ and } \emptyset = 0.5$$

In order to test the effect of uncertainties in the threshold values on the outranking performance of each alternative, a sensitivity analysis is performed; its details are presented in the next subsection.

#### 4.1 Sensitivity analysis

A sensitivity analysis [32-33] helps to study deviations in the outcome parameters of any model due to deviations in input parameter values. One needs to establish the effect of a variation in input variables on output variables. A sensitivity analysis can help the decision-maker to determine which parameters are the key drivers. Here, a sensitivity analysis is done to evaluate alternative wind farm locations according to variations in attribute and sub-criteria weights and threshold coefficients. Variations in input parameter threshold coefficient values (see Table 3) and three sets of attribute weights (see Table 2) are used for the sensitivity analysis. Since too much data was gathered after the sensitivity analysis, the sample final outranking relationship kernel graph obtained for selected pairs of threshold values and corresponding attribute weight sets are presented in Figure 5. Based on the kernel graph, the overall preference order of alternatives corresponding with the obtained changes in threshold values and sets of attribute weights is presented in Table 4.

**Table 4: Preference order of alternative wind farm locations based on kernel graph**

Overall preference order	WFL1	WFL2	WFL3	WFL4	WFL5
	1	1	2	3	4

From Figure 5, one notes that threshold values and attribute weights are sensitive to changes in the outranking relationship graph. The obtained ranking order of alternatives that correspond to changes in threshold values and sets of attribute weights is presented in Table 4. From Table 4, after the sensitivity analysis, it is evident that wind farm location WFL5 is found to be the least preferred other alternatives, while WFL1 and WFL2 are preferred options for the decision-maker over WFL3 and WFL4.

## 5 CONCLUSION

Renewable energies cater for varying global energy demand conditions. But there is risk in changing from an old energy system setup to any new one without prior evaluation. Mostly, in such cases, the alternatives need to be evaluated on multiple performance parameters. As presented in this paper, the Saudi Arabian power energy planners were interested in assessing and ranking wind power plant alternative locations to satisfy the dynamic competitive energy requirements. They identified suitable alternatives. Minimising cost was the priority in any decision analysis. The approach presented here was to show that any assessment of these alternatives needs to take multiple performance criteria into account. The decision managers had wind speed, wind availability, site advantage, terrain details, risk and uncertainty, technology used, third party support, projected demand, type of customers, and government policies as evaluating criteria (see Figure 2).

Using the interactive tool, an alternative detail qualitative and quantitative data collection corresponding with multiple-attributes was done. The results obtained were further subjected to sensitivity analysis.

From the sensitivity analysis it is clear that if, management wishes to set equal weighting for all criteria, WFL2 is the superior choice over the other four locations, and WFL4 and WFL5 are the worst choices. But, when a) high and equal weighting is set to available wind speed, area wind density, and surrounding environmental concerns, b) least and equal weighting is set to investment cost and government policies, and c) average weighting is set to loss, threats/risk associated, power demand, and supply cost, the selection order is found to be WFL1, WFL2, WFL4, WFL3, WFL5. Similarly, when a) high and equal weighting is set to available wind speed, area wind density, investment cost, power demand, and supply cost, b) least and equal weighting is set to loss, threats/risk associated, and c) average weighting is set to government policies and technology used, the ranking order is found to be WFL2, WFL1, WFL3, WFL4, WFL5. Thus, by assessing alternative wind farm locations, decision-makers proposed to select either WFL1 or WFL2.

It is evident that the proposed MCDM approach is preferable because it needs very few controlling factors, compared with other existing multi-criteria approaches. The approach is also easy to understand and is less biased in the decision-making process. The approach is characterised by thresholds and outranking relationships. The thresholds are defined by the decision-makers. The approach also generates a system of binary outranking relationships among the alternatives: the alternative is preferred if, and only if, both the concordance and discordance conditions are satisfied. This approach's major advantage is that it takes into account uncertainty and fuzziness. One disadvantage is that, due to the way preferences are incorporated, the lowest performances under certain criteria are not displayed. Another interesting challenge might be the development of a model to incorporate real-time criteria. In future, one could also verify the consistency of decisions using other multi-criteria approaches.

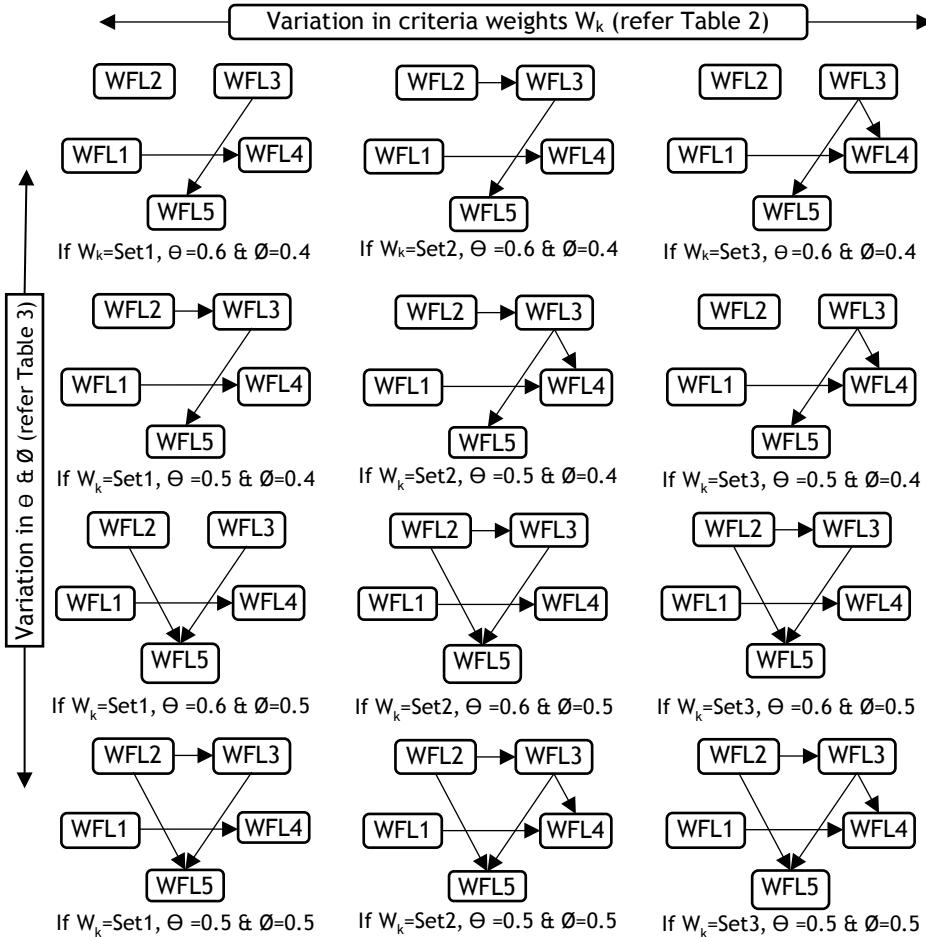


Figure 5: Outranking-relationship Kernel graphs after sensitivity analysis

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