APPLICATION OF PROFITABILITY CONCEPT: A CASE IN THE PLASTIC RECYCLING INDUSTRY

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ABSTRACT

In this article the principles of industrial engineering are applied to maximize the profitability of the recycling industry. A case in the plastic recycling industry is presented to demonstrate the practical application of the financial calculation functions developed in the paper. In particular, the profitability maximization concept for the plastic recycling industry was examined, based on the theory of demand and supply. By estimating the profit realizable on regular as well as high product demand, part of the objective of the paper was achieved. Inventory principles were further applied to determine optimum inventory levels.

OPSOMMING

Die beginsels van bedryfingenieurswese word in die artikel toegepas om die maksimisering van winsgewendheid by herwinbaarheidsvraagstukke te bewerkstellig. 'n Voorbeeld wat voorkom by die herwinbaarheid van plastiek word voorgehou om te toon hoedat finansiële modellering aangewend kan word. Voorraadhouding onder toestande van stabiele en toenemende vraag word behandel en in besonderheid ondersoek.
1. INTRODUCTION

In recent times, recycling and recycling practices have become increasingly important owing to the pressures experienced by industries worldwide [6]. For example, a strong indication of the “end-of-life directives” endorsed by the European Union is that, if resources are not recycled, a period may come when very limited resources are available to humanity. Consequently, we may need to suffer for the shortage of these important resources. With the numerous supports for investment in recycling technology and operation, many industrialists are considering the possible expansion of existing structures and processes in order to maximize profits [27, 28]. With the benefits of saving costs, protecting the environment from pollution, and making maximum use of available resources, international agencies and other stakeholders are also investing in projects that will enhance the promotion of environmental cleanliness through recycling.

Over the last decade, efforts have been made to formalize the economic and financial calculations relating to recycling – and especially plastic recycling, which is the main focus of this paper – through life-cycle approaches [2, 12, 16]. Furthermore, the economics of recycling are constantly debated [11, 20, 21]. The contribution of this paper is to add value to the field of industrial engineering in general through the application of calculation procedures or mathematical methodologies in the plastic recycling industry. The paper presents a clear case study demonstrating the use of the mathematical functions. An overview of selected research articles relating to recycling of different types of materials, including plastics, is presented.

2. RELEVANT LITERATURE

The research methodology for selecting and assessing the papers reviewed here is based on a SWOT-type analysis of the different approaches, which indicated the need for a new financial model. The SWOT-type analysis also reveals the different approaches that are considered for inclusion in the development of such a new model. The literature reviewed here relates to the current theoretical modelling of recycling in the fields of “designing for recycling” and “life-cycle costing” [3, 8, 9, 22].

Recycling has numerous advantages. Waste from recycling is usually channelled into refuelling the recycling process or sold to other industries as a useful source of fuel for operations. Therefore, with recycling, new ideas and products are created. Such products tend to be more suitable for application than those created from raw materials. Unfortunately, recycled materials may not be ideal for the purpose of materials made from raw materials. The process of recycling is characterised by a lack of technical know-how, skilled and trained personnel, and facilities. Another threat to recycling is that it is impossible to recycle some materials. Also, a lot of time, dedication, and extensive research are needed to determine how best to recycle material. Another threat is that there are few experts in the field of recycling in underdeveloped countries. Where they exist, the technology may not be technically sound. In Table 1 below, we present the SWOT-type analysis to reveal the strengths, weaknesses, opportunities, and threats of the available approaches in the literature on recycling.
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<th>S/No.</th>
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<td></td>
<td></td>
<td>Focuses attention on large quantities of printed circuit boards (PCBs) being consigned to landfill by electronics manufacturing firms.</td>
<td>Work does not reflect profitability elements</td>
<td>Approach could also be extended to other materials such as electromechanical systems, computer accessories, automobile components, etc.</td>
<td>Low awareness and non-challant attitude from members of the public</td>
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<td>New methodologies for dealing with end-of-life circuit boards are identified as a priority issue.</td>
<td>Only a small part (15%) of total PCB scrap currently generated is subject to any form of recycling. A major part is consigned to landfill.</td>
<td>It is an environmental pollution reduction strategy. As part of municipal waste that is properly disposed of, it helps to reduce public waste that would constitute a health hazard</td>
<td>The people and government’s willingness to implement work, but then discarding it midway.</td>
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<td>Reports on study carried out to identify the technologies and processes that can be used to recycle materials from end of life PCBs.</td>
<td>Reports on study carried out to identify the technologies and processes that can be used to recycle materials from end of life PCBs.</td>
<td>Achieving increase in the level of recycled end-of-life electronics products, with focus on attaining complete recycling of all electronics products</td>
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Table 1: Strength Weakness Opportunity and Threat (SWOT) analysis of the different approaches
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<td>3.</td>
<td>Smith et al. [25]</td>
<td>It surveys several schemes that collect plastic bottles for recycling in the UK. An Environment Act imposes a legal requirement for plastic packaging to be recycled. A national target of 15% recycling of plastic packaging waste by 2001 was implemented.</td>
<td>This survey project did not investigate modelling. Further assistance was required in order to meet the national target. The profitability of financial functions relating to plastic recycling was not identified by the authors.</td>
<td>It highlights various recycling schemes in the UK with respect to their distribution, efficiencies, and types. Other areas such as effectiveness, acceptance, and control could be further examined.</td>
<td>The people’s adherence to or apathy towards the Environment Act will go a long way to determining its success or failure.</td>
</tr>
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<td>4.</td>
<td>Treloar et al. [27]</td>
<td>Focuses on waste minimization strategies and use of recycled materials for the construction of residential buildings. Embodied energy is a useful indicator of resource value. This paper thoroughly identifies the various types of waste that were generated from the construction of a typical standard house. Study discovers that amount of wasted material was less than that found previously by others in cases in capital cities. Innovative waste management strategies aimed at reducing the resource requirement of the construction process.</td>
<td>Cost and embodied energy savings from using materials with recycled content were potentially more beneficial in terms of embodied energy and resource depletion than waste minimization strategies.</td>
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| 5.   | Lee et al. [14] | Recycling is a major source of employment and research opportunities.  
Critical analysis of recycling potential of plastic waste generated by healthcare facilities through the evaluation of disposal costs, plastic contents, components, sources, and amount of medical plastic waste.  
It cites some methods to increase or improve the recycling of medical plastic waste.  
It predicts recycling becoming a major sector in many economies of the world in the years to come; making a significant impact on both the environment and human lives. | No consideration is given to profitability measures of plastic recycling system. | - | - |
| 6.   | Gobin and Mano [6] | It possesses the potential to become a commercially viable recycling process.  
This method exposes the recycling process as important in helping in research for suitable materials, better and more efficient industrial processes.  
Some recycled materials, such as pillard clays, offered about the same performance as fresh samples. | High initial cost involved in setting up recycling plants.  
A lot of research must be carried out to discover the best recycling modes for material. | - | - |

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<td>7.</td>
<td>Price and Donald [19]</td>
<td>Discourse is based on real-life cases of 3M life cycle management implementation.&lt;br&gt;Its significance pushes the responsibility of manufacturers beyond the factory environment to include product use by customers and disposal of products.&lt;br&gt;It highlights environmental, health and safety (EHS) opportunities.&lt;br&gt;Identifies competitive market advantages resulting from superior performance.&lt;br&gt;It manages a product’s EHS risks as well as resources and energy use throughout a product’s life cycle.&lt;br&gt;It is a means of reducing environmental pollution.&lt;br&gt;The recycled products are modified, thus having a wider range of use than the original product.&lt;br&gt;Reduces overall expenditure in production, and it is highly profitable.&lt;br&gt;Process consists of simple steps to follow.</td>
<td>No relation to the profitability concept in plastic recycling.&lt;br&gt;Recycling may not reduce overall degradation of environment if other forms of pollution are not controlled.</td>
<td>The modification of recycled products explores the opportunity to locate some products that will meet some demands.</td>
<td>Some products are such that it is difficult for the manufacturer to exercise control over their use by the consumer – e.g. firearms, drugs, etc.</td>
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<td>8.</td>
<td>Lawson et al. [13]</td>
<td>Detailed analysis of construction and demolition waste (C &amp; D waste) generated annually to the tune of 53.5Mt; of which 51% went to landfill, 40% was used for land reclamation and only 9% was crushed for future use or directly recovered.&lt;br&gt;Improved sampling procedures and recommendations for risk assessment for the reuse of C and D waste were being prepared.&lt;br&gt;Attitudes or preferences shifting towards disposal on site.</td>
<td>C &amp; D waste may be contaminated through spillage from industrial processes or contact with contaminated land.&lt;br&gt;No guidelines on how to classify C &amp; D waste as contaminated, nor on risk management for contaminated C &amp; D waste.&lt;br&gt;New taxes made disposal of C &amp; D waste to landfill uneconomical.&lt;br&gt;Low grade ‘land-modeling’ recycling is increasing.</td>
<td>To prepare guidelines on C &amp; D waste classification.</td>
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<td>9.</td>
<td>Romualdo <em>et al.</em> [23]</td>
<td>Investigates recycling of granite industry waste from the northeast region of Brazil; samples of wastes of several granites companies located there were collected. Waste could be used in substitution of conventional raw materials in ceramic formulations in proportions up to 50%. This is important in saving traditional raw material in the region. Aims at the possibility of using sawing granite waste as alternative ceramic raw materials for the production of bricks and roof tiles. Samples of sawing granite wastes were submitted for technological tests revealing waste having size, distribution and composition similar to conventional non-plastic ceramic raw materials.</td>
<td>They discover that solid wastes are one of the worst problems in the world today, owing to increase in volume and environmental contamination.</td>
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<td>10.</td>
<td>Chen [1]</td>
<td>Investigates the development of integrated design for disassembly and recycling in concurrent engineering. Notes previous environment revolution addressing waste reduction at the source. Cites previous measures aimed at cleaning up hazardous waste from contaminated sites and natural resources. Proffers effective methods, such as the design of products that promote disassembly, re-use and recycling. Encourages the design of environmentally friendly products by applying axiomatic design to develop integrated, acceptable, and best designs.</td>
<td>Annually, high disposal costs are incurred worldwide in environmental protection efforts.</td>
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Table 1(cont’d): Strength Weakness Opportunity and Threat (SWOT) analysis of the different approaches
3. REGULAR DEMAND

From the basic knowledge acquired from economics, the flow rate $Q$, which is a measure of the quantity of recycled product, is a function of the price at which it was sold, i.e. $QR = f(Sp)$. When the quantity recycled increases, the overall selling price may increase, but the selling price per unit will reduce. This can be graphically represented as shown below (Figure 1).

![Figure 1: Recycled quantity and time (regular demand)](image)

$SP = \text{selling price per item at a particular instance}$

$QR = \text{quantity recycled at that instance}$

The main reason for establishing a business is to make a profit, so as to increase the business capital and provide income to the owner of the business. The greater the quantity recycled for sale, the higher the profit. Profit is the excess of price over cost price, i.e.:

Profit, $X = \text{Selling Price (SP)} – \text{Cost Price (CP)}$

But, $\text{Selling Price (SP)} = \text{Selling Price per unit (Sp) x Quantity Recycled (QR)}$

Cost Price (CP) = Cost Price per unit (Cp) x Quantity Recycled (QR)

Therefore, $\text{Profit, } X = (Sp \times QR) – (Cp \times QR) = (Sp – Cp)QR$

3.1 Definition of Terms

(i) $Sp$ is the selling price per item of the quantity of plastic wastes recycled. The selling price could vary depending on the cost price at the time and the choice of the recycler.

(ii) $Cp$ is the cost price per item of the quantity of plastic wastes recycled. This would be based on a peripheral computation to be carried out by the recycler. Consideration should be given to all expenses incurred directly during the recycling process. This includes collection of plastic wastes, size reduction
(cutting and shredding), separation or sorting, cleaning and drying, etc. Other expenses that are indirectly incurred include salaries and wages, rent, depreciation of machines and equipment, sundry expenses, etc.

(iii) \( Q_R \) is the quantity of plastic waste recycled. The quantity recycled can be determined by the application of the model which helps to assign values to the recycled quantities – i.e.

Also, let

\[
D = \text{screw diameter}; \\
H = \text{channel depth in the metering zone}; \\
B = \text{flow width} \\
W = \text{channel width parallel to the screw axis}; \\
\theta = \text{Helix angle of the screw} \\
N = \text{screw speed in revolutions per second (rps)}; \\
V = \text{linear velocity}
\]

\[
Q_R = \frac{\text{volume flow rate (Q in m}^3/\text{s}) \times \text{period (T in sec)}}{\text{volume (V in m}^3/\text{item})}
\]

\[
= \left[ \frac{\pi Dh W N \cos^2 \theta}{2} \cdot \frac{h^3 WP \cos \theta}{12 L \mu a} \right] \frac{T}{V} \text{ item}
\]

where \( T = \text{period between the beginning of recycling and the expected completion time} \)

\[
V = \text{volume that makes each item of the recycled product.}
\]

Therefore,

\[
\text{Profit, } X = \left[ (S_P - C_P) \frac{\pi Dh W N \cos^2 \theta}{2} \cdot \frac{h^3 WP \cos \theta}{12 L \mu a} \right] \frac{T}{V}
\]

4. UPSURGE IN DEMAND

In the recycling industry, it is usually at certain periods that there is a sudden upsurge in demand from customers. This upsurge could be weekly, monthly or even yearly. Upsurge is a specific problem in the recycling industry [7, 15]. For instance, in the case of a weekly demand cycle, it is likely that demand would rise on Fridays for various parties.

Upsurge in the industry could happen in two ways:

(i) Immediate increase in demand (order)
(ii) Future (unforeseen) increase in demand (order)
Immediate increase in demand

If a customer usually demands $Q_R$ items, the company probably recycles just that quantity. But with an increase in demand – say, $Q_{R2}$ items – the company must meet it in order not to lose customers or future sales.

The proposed model would help suppliers to meet such situations. With slight adjustments in some of the parameters, the change in quantity recycled could be expressed in Figure 2.

Considering the profit before ($X_1$) and after ($X_2$) increase:

**Profit before ($X_1$):**
\[
X_1 = SP_1 - CP_1 = (SP_1 - CP_1)Q_{R1}
\]

where
\[
Q_{R1} = \frac{Q_1 x T}{T}
\]

\[
x_1 = (SP_1 - CP_1)x \left( \frac{Q1T}{V} \right) = \left[ (SP_1 - CP_1) \right] \left( \frac{\pi D h_1 W_2 N_2 \cos^2 \theta_1}{2} \cdot \frac{h_1^3 W_2 P_1 \cos \theta_1}{12 L_1 \mu a_1} \right) \left( \frac{T}{V} \right)
\]

**Figure 2: Recycled quantity and time (upsurge conditions)**

### 4.1 Definition of terms

(a) (i) All terms are the same as those described under regular demand. Only the subscript 1 indicates the original value of all the parameters, before change.

(ii) Profit after ($X_2$)
\[
X_2 = SP_2 - CP_2 = (SP_2 - CP_2)Q_{R2} = \left[ (SP_2 - CP_2) \right] \left( \frac{\pi D h_2 W_2 N_2 \cos^2 \theta_2}{2} \cdot \frac{h_2^3 W_2 P_2 \cos \theta_2}{12 L_2 \mu a_2} \right) \left( \frac{T}{V} \right)
\]

(b) (i) $SP_2$ is the selling price per item of the increased quantity ($Q_{R2}$). In most cases, this price is slightly lower than the original selling price per item ($SP_1$).
It is usually a percentage of \( S_{P1} \) – i.e. \( S_{P2} = aS_{P1} \). The percentage “a” depends on the recycler.

(ii) \( C_{P2} \) is the cost price per item of the increased quantity \( Q_{R2} \). As explained earlier, computation of the cost price per item depends on the expenses incurred both directly and indirectly. Direct expenses on collection, reduction, sorting, etc. would definitely increase as long as the quantity recycled increases. However, indirect expenses such as salaries, wages, rent, etc. might not necessarily change. Similarly, \( S_{P2} \), the cost price per item, would be slightly lower than the original cost price per item. It is also a percentage of \( C_{P1} \) – i.e. \( C_{P2} = bC_{P1} \). It should be noted that the cost incurred due to changing any of the parameters falls under direct expenses.

(iii) One or more of the eight parameters that make up \( Q_{R2} \) could be adjusted, depending on the recycler’s choice, policy, and strategy in meeting the increased quantity. This implies that some of these parameters would not change, since changing all would increase the cost. This would not favour the recycler’s quest for profit.

(iv) Period (T) and volume (V) would not change. The period and volume remain the same for either the original quantity or the increased quantity.

(c) The increase in profit as a result of meeting the increased quantity \( Q_{R2} \) can be measured by:

\[
X_0 = X_2 - X_1 = \left[ (S_{P2} - C_{P2}) \left( \frac{\pi D_2 h_2 W_2 N_2 \cos^2 \theta_2}{2} - \frac{h_2^3 W_2 P_2 \cos \theta_2}{12 L_2 \mu a_2} \right) \right] - \left[ (S_{P1} - C_{P1}) \left( \frac{\pi D_1 h_1 W_1 N_1 \cos^2 \theta_1}{2} - \frac{h_1^3 W_1 P_1 \cos \theta_1}{12 L_1 \mu a_1} \right) \right] \frac{T}{V}
\]

Simplifying this expression, we have

\[
X_0 = \left[ (S_{P2} - C_{P2})Q_2 - (S_{P1} - C_{P1})Q_1 \right] \frac{T}{V}
\]

\textit{Unforeseen increase in demand}

In this case, the increase in demand lies in the future, but the company presumes that it will occur at some time. Therefore the company recycles a greater quantity than is actually needed at that time. The effect of this on the increase in profit \( (X_0) \) is seen in the need to keep the excess recycled products in store. The cost of keeping the excess in store includes:

(a) Storage charges – i.e. rent, lighting, insurance, and security.
(b) Interest on capital investment on the stored products.

\textbf{4.2 Storage cost analysis}

The cost of holding items in storage and of interest on the money invested in the items is directly proportional to the quantity of the items \( Q_{RS} \). This quantity \( Q_{RS} \) is
the difference between the actual recycled product $Q_{R2}$ and the present demand $Q_{R1}$ – i.e.:

$$Q_{RS} = Q_{R2} - Q_{R1} = (Q_2 - Q_1) \frac{T}{v}$$

Assuming that the average quantity of items in store is $\frac{Q_{RS}}{2}$, and that $H$ represents the holding cost per item per period (t), then Holding Cost (HC) = $\frac{H Q_{RS}}{2}$.

Also, let $CP = \text{cost price (investment)} = C_{P2} - C_{P1}$, and $\tau = \text{interest rate of money invested in } Q_{RS}$.

Therefore, Interest Charge (IC) = $(C_p) x (i) x \frac{Q_{RS}}{2} = \frac{i C_p Q_{RS}}{2}$

Total Storage Cost, $T_{SC} = HC + IC = \frac{H Q_{RS}}{2} + \frac{i C_p Q_{RS}}{2} = [H + i C_p] \frac{Q_{RS}}{2}$

but $H = \frac{h}{t}$

where $h = \text{holding cost per item}$

$t = \text{time the excess quantity } Q_{RS} \text{ spends in the store.}$

Therefore $T_{SC} = \left( \frac{h}{t} + i C_p \right) \frac{Q_{RS}}{2}$

**Maximum profitable period (t) of storage**

It is possible for the quantity $Q_{RS}$ to be stored and sold when there is an upsurge in demand, but for the company still to run at a loss. It is important to note that the increase in profit $X_0$, must be more than the total storage cost $T_{SC}$ for profit – i.e. $X_0 > T_{SC}$. For easy assessment in the recycling industry, it is best stated in terms of the maximum time that the company should keep the items in store. To obtain the maximum time that the items can be stored, it is best to equate the increase in profit, $X_0$, to the total storage cost, $T_{SC}$.

Therefore,

$$\left[ (S_{P2} - C_{P2})Q_2 - (S_{P1} - C_{P1})Q_1 \right] \frac{T}{v} = \left( \frac{h}{t} + i C_p \right) \frac{Q_{RS}}{2}$$

$$\frac{h}{t} + i C_p = \frac{2T}{VQ_{RS}} \left[ (S_{P2} - C_{P2})Q_2 - (S_{P1} - C_{P1})Q_1 \right]$$
\[ \frac{h}{t} = \frac{2T}{VQ_{RS}} \left[ (S_{p2} - C_{p2})Q_{2} - (S_{p1} - C_{p1})Q_{1} \right] - iC_{p} \]

\[ \frac{h}{t} = \frac{2T}{VQ_{RS}} \left[ (S_{p2} - C_{p2})Q_{2} - (S_{p1} - C_{p1})Q_{1} \right] - iC_{p} \]

\[ t = h \left[ \frac{2T}{VQ_{RS}} \left[ (S_{p2} - C_{p2})Q_{2} - (S_{p1} - C_{p1})Q_{1} \right] - iC_{p} \right]^{-1} \]

but \[ H = \frac{h}{t} \]

where \( h \) = cost of holding in storage
\( t \) = time the excess quantity \( Q_{RS} \) spends in store per year.

Since the storage time might not be measured in years, it is reasonable and practicable to reduce it to weeks.

1 year = 52 weeks; \( t \) years = \( \frac{52}{1} \times t \) weeks = 52t weeks

\[ \therefore 52t = h \left[ \frac{2T}{VQ_{RS}} \left[ (S_{p2} - C_{p2})Q_{2} - (S_{p1} - C_{p1})Q_{1} \right] - iC_{p} \right]^{-1} \]

\[ t = \frac{h}{52} \left[ \frac{2T}{VQ_{RS}} \left[ (S_{p2} - C_{p2})Q_{2} - (S_{p1} - C_{p1})Q_{1} \right] - iC_{p} \right]^{-1} \]

\[ t \text{ (in wks)} = \frac{h}{52} \left[ \frac{2T}{VQ_{RS}} \left[ (S_{p2} - C_{p2})Q_{2} - (S_{p1} - C_{p1})Q_{1} \right] - iC_{p} \right]^{-1} \]

5. CASE STUDY

In order to explain the practical application of the model developed in this work, the case of a plastic recycling plant situated in a major city in southern Nigeria is used as an example. The process consists of two main sub-processes: pre-recycling, and the main recycling.

The pre-recycling processes are: (i) collection; (ii) size reduction; (iii) separation or sorting; and (iv) cleaning and drying. The major polymer recycling process is extrusion. Extrusion is a polymer conversion operation. It is employed to recycle and homogenize the plastic, and produce a material that is easy to work with to produce new products. In this process, a solid thermoplastic material is melted, forced through a die of the desired cross-section, and cooled. The devices used to carry out extrusion are called extruders.

Although there are many types of extruders, the most common is the single-screw extruder. This consists of a screw in a metal cylinder or barrel. The barrel is
surrounded by electric heater bands and fans. The screw is connected through a
thrust bearing and gearing to a drive motor that rotates the screw in the barrel. A
conical hopper is connected to the feed throat, a hole in the barrel near the drive end
of the screw. The opposite end of the barrel is fully open and exposes the tip of the
screw. A die is connected to the “open” end of the extruder. During extrusion, solid
plastic in the form of pellets is fed from the hopper, through the feed throat of the
extruder, and into the extruder barrel. The pellets fall on to the rotating screw and are
packed in the first section of the screw (called the feed zone). The packed pellets are
melted as they travel through the middle section (called the transition zone) of the
screw, and the melt is mixed in the final section (called the metering zone). Although
the heater bands and cooling fans maintain the barrel at a set temperature, conduction
from the barrel walls provides only 30% to 40% of the energy required to melt the
resin. The remaining energy is generated from the mechanical motion of the screw;
this is called viscous dissipation.

Pressure generated in the metering zone of the extruder screw forces the melt through
the breaker plate and die. The breaker plate provides a seal between the extruder and
die, and converts the rotational motion of the melt (in the extruder) to linear motion
(for the die). The breaker plate also holds a screen pack that filters the melt. The die
forms the melt into the desired shape. Ancillary equipment is used to cool the melt
and pull the cooled material away from the die.

Three types of flow exist in a single-screw extruder. The rotating screw pushes
material along the walls of the stationary barrel (cylinder), which creates drag flow
(Q_D). This drag flow provides the forward conveying action of the extruder, and in
the absence of a die, is effectively the only flow present. The addition of a die
restricts the open discharge at the end of an extruder and produces a large pressure
gradient along the extruder. Since the pressure is greatest just before the die, this
head creates the other two flows, pressure flow (Q_P) and leakage flow (Q_L). In
pressure flow, the head pressure forces the melt to rotate in the channels of the
extruder screw. Leakage flow occurs when the head pressure forces melt back over
the flights of the screw. Since these are both counter-motions of the melt, pressure
and leakage flow are often lumped together as ‘back flow’. During normal extruder
operation, drag flow conveys the polymer along the barrel walls, whereas pressure
flow forces the material near the screw back towards the hopper. A simple
mathematical modelling of extrusion can be made by assuming the following
conditions:

- the extruder is at steady state
- the melt is Newtonian (viscosity does not change with changes in shear rate)
- the melt is isothermal (at a constant temperature) and
- the metering zone makes the only contribution to output.

Thus the net output, Q, of the extruder can be expressed as:

\[ Q = Q_D - Q_P - Q_L \]
From our assumptions, the metering zone of the screw is expected to contain almost 100% melt and be at an almost constant temperature. Consequently, if an estimation of the output from this zone is possible, then the output from the whole extruder can be estimated, considering the geometry of the flow in the metering zone of an extruder screw.

6. DISCUSSION OF RESULTS

The major aim of the recycling profitability measure is to assist recyclers in quantifying the profit they could make in a particular recycling production. It gives them room to evaluate the increase in profit. Furthermore, an expression was derived to assist recyclers in determining how long recycled products could be allowed to remain in storage before the excess profit would be lost. All of these were achieved by applying various principles from economics and operations research – for example, the theory of demand and supply, and the principles of inventory. With the recycler’s ability to assign numerical values to the various parameters in the equation, the possibility of determining the increased profit and the maximum time in store is very high.

7. CONCLUSIONS

In this work, some industrial engineering tools were applied to the plastic recycling industry in order to improve organizational performance by improving profitability. In particular, a case study demonstrated the applicability of the presented financial calculation model. The case revealed a situation in which an upsurge in product demand affected the profitability of the organization. Having demonstrated the feasibility of applying the financial model in a real life situation, a wide array of opportunities for future development of the financial calculation functions was presented.

Every establishment aims at making profit for the purpose of expansion. With this in mind, this financial model has been examined to see how it could be useful in estimating the profit made on a particular quantity being recycled within a particular period. Since the model has the benefit of assisting the industry to increase the quantity being produced within the same period, it was considered necessary to examine the additional profit that the industry could make by meeting an upsurge in demand. A mathematical expression to assist in this was developed. This expression is useful when the increase in demand is immediate. In a situation where the increase in demand is the quantity recycled and kept in store, additional cost is incurred, resulting in reduced additional profit.

In the long run, the industry might run at a loss if the additional cost $T_{sc}$ equals the additional profit $X_0$. In order to keep the industry on alert, so as not to lose in the long run, the maximum profitable period, $t$, for keeping extra recycled quantities in storage is expressed in weeks.
The proper application of this measure will always help the industry to make additional profit, even when extra quantities of products are recycled and kept in storage in order to meet unforeseen increases in demand.

In decision science, the use of the analytical hierarchy process (AHP) in prioritizing resources for recycling operations will bring immense benefits to researchers and practitioners. Other scholars could apply the newly-developed hybrid structural iteration matrix (HSIM) to the model presented in this work. The application of neurofuzzy modeling may stimulate long-lasting research, since new dimensions of recycling research would emerge.

An immediate follow-up study should be made of the sensitivity analysis and test of the model presented. The sensitivity should reflect the degree of responsiveness of model variables and parameters to changes in their values. Such an evaluation should reflect which of the model’s parameter and variables are susceptible to changes, and which ones are the most sensitive.

Another area for further extension of the model is the development of optimized quantity for the model. A first instance may be the application of Lagrangian’s multiplier to the existing model. Other optimization techniques may assist here too.

Furthermore, future extensions of the current model could incorporate some soft computing tools. A wide variety of such tools are available. Examples include fuzzy logic, genetic algorithm, artificial neural network, and neurofuzzy. Another dimension in improving the proposed financial model is the application of the concept of calculus. In particular, the calculus of several variables may be immediately applied. Further work could investigate modifying the model to form a continuous function. An investigation into case studies that show a comparative analysis might be interesting.

In conclusion, we have presented a financial calculation model capable of stimulating future research. We hope that the work serves as a guideline for new entrants.

8. REFERENCES


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